

# Solid State Power Combiners for Accelerator Applications

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## Power Amplifiers

#### Klystrons (Tube Amplifiers)

High Power (MegaWatts) In use for almost a century Prohibitively Expensive



#### Solid State Amplifiers

Lower Power (KiloWatts) Requires a combiner Predictable Performance



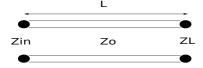
## Transmission Line Theory

$$V(z) = V_0^+ e^{-j\beta z} + V_0^- e^{j\beta z}$$

$$I(z) = \frac{V_0^+}{Z_0} e^{-j\beta z} - \frac{V_0^-}{Z_0} e^{j\beta z}$$

$$\Gamma = \frac{V_0}{V_0^+} = \frac{Z_L - Z_0}{Z_L + Z_0}$$

$$Z_{in} = Z_0 \frac{Z_L + jZ_0 tan(\beta I)}{Z_0 + jZ_L tan(\beta I)}$$



## Coaxial Tree Design

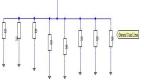
$$Z_0 = \sqrt{Z_{in}Z_L} \ (\frac{\lambda}{4} \ Transformer)$$

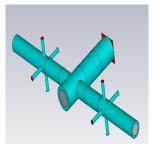
$$Z_{in} = jZ_0 tan(\beta I)$$
 (Short – Circuit St  
 $S_{11}$  (dB) =  $20log(\Gamma)$ 









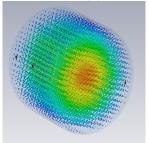


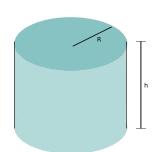
## Cavity Combiner Design

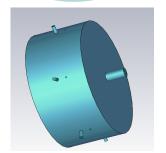
$$f_{m,n,p} = \frac{v_p}{2\pi} \sqrt{\left(\frac{X_{m,n}}{R}\right)^2 + \left(\frac{p\pi}{h}\right)^2}$$

$$Q = \frac{2\pi f_0 U}{P}$$

$$\beta = \frac{Q_0}{Q_{\text{ext}}}$$

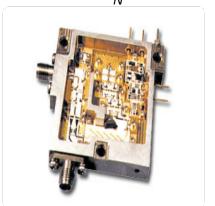


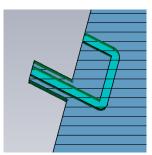


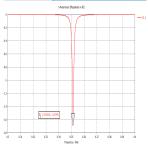


## Input Coupler Design

$$\beta = 100$$
 
$$\Gamma = \frac{1 - N}{N}$$







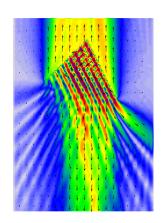
#### **Evaluations of Power**

$$\vec{S} = \frac{1}{2}\vec{E} \times \vec{H}^*$$

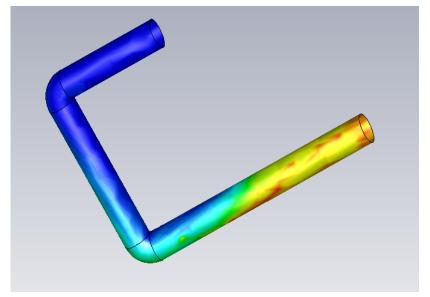
$$P = \int \vec{S} \cdot d\vec{S}$$

$$Loss = \frac{1}{2}R_s \int \vec{H} \cdot \vec{H}^* d\vec{S}$$

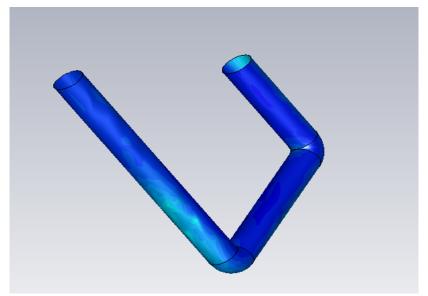
$$R_s = \sqrt{\frac{\omega\mu}{2\sigma}}$$



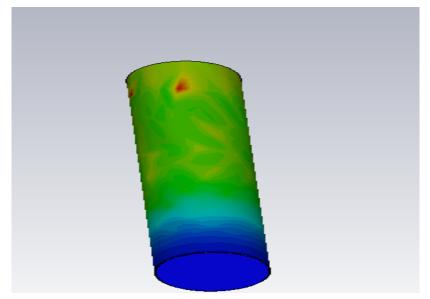
## Input Coupler Power Flow



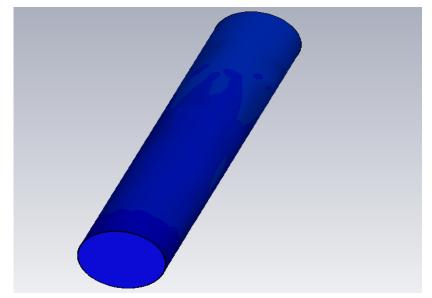
# Input Coupler Loss



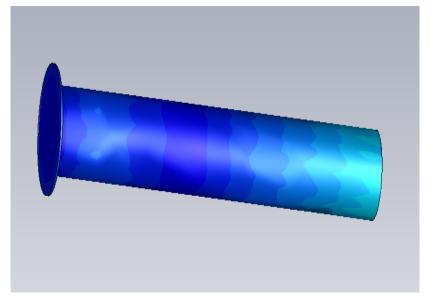
## Coaxial Output Coupler Power Flow



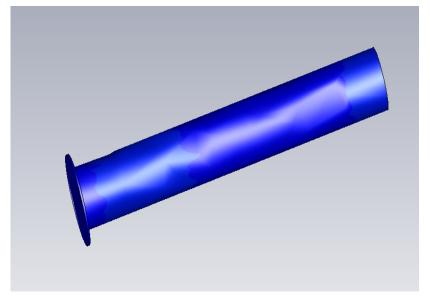
## Coaxial Output Coupler Loss



# Cylindrical Output Coupler Power Flow



# Cylindrical Output Coupler Loss



#### Acknowledgements

Thank you to everyone who made this possible. Special thanks to Geoff Waldschmidt and Doug Horan.

Good Luck Everybody.